# Heuristic function

My heuristic function calculates the sum of six terms that each give some weight to specific qualities in a state of the game.

Next, I will go into detail about how each term is calculated.

## Gradient cell weight

In 2048, it is a good idea to build against one of the sides, i.e. keep the largest tiles on one side. The cell weight concept is to calculate a variable that is the sum of each tile value times a weight that is specific for that position. For example, here is the gradient matrix that gives more weight to tiles in the upper area:

However, in bad states it is good for the AI to have some flexibility in choosing a new side to build against, rather than enforcing the same side as before. Therefore, I figured that it’s a good idea to calculate one score for each gradient direction, and then choose the maximum of the four scores to be the cell weight term.

Further, it’s obviously good to favor few large tiles over many medium tiles. Therefore, I’ve modified the concept slightly: each tile value is raised to the power of 1.3 before it’s multiplied with the cell weight.

Where is defined as the value of the tile in the i-th row in the j-th column and where and are created by the same concept as , i.e. a matrix with values ranging from 1 to 4 according to a gradient in the given direction.

Finally,

## Empty cells

I added this term to avoid a cramped situation with a small number of empty tiles. Larger scores are given to states with a larger number of empty tiles.

Where is defined as the value of the largest tile

## Smoothness

Two adjacent equal tiles means that they can be merged, and that is a good thing. The concept of smoothness tries to boil this down to a number. This number becomes larger when there are more equal tiles adjacent to each other. Smoothness is calculated for each row and for each column, and finally those numbers are summed to become the smoothness term.

Where is the value of the k-th tile in the row or the column.

## Monotonicity

Monotonicity is the concept of having a row or a column where the values are ordered in either ascending order or descending order. The idea is to put tiles that are almost the same next to each other, because when a tile gets merged into the smallest of the two, then the two tiles become equal, and are ready to merge. This way, having a monotonic row or a column means that one can merge many tiles consecutively in order to get a single, large tile. For example, the row [256, 128, 64, 64] can get a 512 tile by moving left three times.

Observe that in the calculation of monotonicity, a smaller score is given for ordered values that have a large gap in difference, due to the way works.

## Max tile value

This term is simply the value of the largest tile in the current state. It’s useful because it gives extra weight to moves that merge two tiles to get a tile that is larger than all the others.

## Max tile in corner

As stated in the assignment text, it’s a good idea to have the largest tile in a corner. This term gives such states extra weight.